



K17U 2546

Reg. No. :

Name :

I Semester B.Sc. Degree (CBCSS – Reg./Supple./Improv.)

Examination, November 2017

(2014 Admn. Onwards)

COMPLEMENTARY COURSE IN MATHEMATICS

1C01 MAT-CS : Mathematics for Computer Science I

Time : 3 Hours

Max. Marks : 40

SECTION – A

All the first 4 questions are compulsory. They carry 1 mark each.

1. Find $\frac{dy}{dx}$ when $x = t^3$ and $y = t^2 - t$.

2. Find the derivative of $\ln(\sinh x^4)$.

3. If $z = x/y$, find $\frac{\partial z}{\partial y}$.

4. Find an equation for the circular cylinder $4x^2 + 4y^2 = 9$ in cylindrical coordinates.

(1×4=4)

SECTION – B

Answer any 7 questions from among the questions 5 to 13. These questions carry 2 marks each.

5. If $y = x^2 \cos x$, show that $x^2 y_2 - 4xy + (x^2 + 6)y = 0$.

6. Find the n^{th} derivative of $y = \frac{x+1}{x^2-4}$.

7. If $\cos^{-1}\left(\frac{y}{b}\right) = \log\left(\frac{x}{n}\right)^n$, prove that $x^2 y_{n+2} + (2n+1)xy_{n+1} + 2n^2 y_n = 0$.

8. Find the 1027th derivative of $g(x) = \cos x$.

9. Verify Rolle's theorem for $f(x) = \log(x^2 + 2) - \log 3$ on $[-1, 1]$.

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10. Evaluate $\lim_{x \rightarrow \pi} \frac{x \cos x + \pi}{\sin x}$.
11. If the sides and angles of a plane triangle ABC vary in such a way that its circum radius remains constant, prove that, $\frac{\delta a}{\cos A} + \frac{\delta b}{\cos B} + \frac{\delta c}{\cos C} = 0$, where δa , δb and δc denote small increments in the sides a, b and c respectively.
12. Verify Euler's theorem when $f(x, y) = ax^2 + 2hxy + by^2$.
13. Find the radius of curvature at any point (x, y) of the curve, $y = a \log \sec(x/a)$.

(2×7=14)

SECTION - C

Answer **any 4** questions from among the questions 14 to 19. These questions carry **3 marks each**.

14. Prove that $f\left(\frac{x^2}{1+x}\right) = f(x) - \frac{x}{1+x} f'(x) + \frac{x^2}{(1+x)^2} \frac{f''(x)}{2!} + \dots$
15. Evaluate $\lim_{x \rightarrow \pi/4} (\tan x)^{\tan 2x}$.
16. Verify Lagrange's mean value theorem for the function $f(x) = (x-4)(x-6)$ in $[4, 10]$.
17. If $u = 3(lx + my + nz)^2 - (x^2 + y^2 + z^2)$ and $l^2 + m^2 + n^2 = 1$, show that $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} = 0$.
18. Show that the chord of curvature through the pole of the equiangular spiral $r = ae^{\theta \cot \alpha}$ is $2r$.
19. What do the following equations represent in three dimensional geometry ?
- $xyz = 0$ in Cartesian coordinates.
 - $\rho = 0$ in spherical coordinates.
 - $\phi = 0$ in spherical coordinates.

(3×4=12)



SECTION – D

Answer **any 2** questions from among the questions **20** to **23**. These questions carry **5** marks **each**.

20. Use Maclaurin's theorem to find the expansion of $\log(1+e^x)$ in ascending powers of x to the term containing x^4 .

21. Find the intervals in which the function given by

$$f(x) = \frac{3}{10}x^4 - \frac{4}{5}x^3 - 3x^2 + \frac{36}{5}x + 11 \text{ is}$$

- a) strictly increasing
- b) strictly decreasing.

22. Find the centre of curvature of the four cusped hypocycloid, $x = a\cos^3\theta$, $y = a\sin^3\theta$.

23. a) Convert the point $(1, -1, -\sqrt{2})$ from Cartesian to spherical coordinates.

b) Find an equation in spherical coordinates for the surface $3x^2 - x + 3y^2 + 3z^2 = 0$.

(5×2=10)