

Reg. No.:....

Name:.....

IV Semester B.Sc. Degree (CBCSS – 2014 Admn. – Regular) Examination, May 2016 COMPLEMENTARY COURSE IN MATHEMATICS 4C04 MAT-PH: Mathematics for Physics and Electronics – IV

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Time: 3 Hours Max. Marks: 40

SECTION-A

All the first 4 questions are compulsory. They carry 1 mark each.

- 1. Find ∇ f where $f(x, y) = \frac{x}{y}$.
- 2. Evaluate $\int_{C} (dx + dy)$ where C is a smooth curve from point (1, 2) to (3, 4).
- 3. For the differential equation $y' = x + y^2$, find the first approximation to y given by Picard's method subject to the condition y = 1 when x = 0.
- 4. What is an initial value problem?

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SECTION-B

Answer any 7 questions from among the questions 5 to 13. These questions carry 2 marks each.

- 5. Find the tangent to the ellipse $\frac{1}{4}x^2 + y^2 = 1$ at $P: (\sqrt{2}, 1/\sqrt{2})$.
- 6. Find the directional derivative of $f(x, y, z) = 2x^2 + 3y^2 + z^2$ at P: (2, 1, 3) in the direction of a = [1, 0, -2].

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- 7. Find curl and divergence of the vector field $v = [e^x, e^{xy}, e^{xyz}]$.
- 8. Calculate $\int_C F(r)$ dr where $F = [x^2, y^2, 0]$, C the semicircle from (2, 0) to (-2, 0), $y \ge 0$.
- 9. Use Green's theorem to evaluate $\int_C F(r)$. dr counterclockwise around the boundary curve C of the region R, where F = [y sin x, 2x cos y], R the square with vertices $(0, 0), (\pi/2, 0), (\pi/2, \pi/2), (0, \pi/2)$.
- 10. Evaluate $\iint_S F \cdot n \, dA$ where $F = [x^2, 0, 3y^2]$ and S is the portion of the plane x + y + z = 1 in the first octant.
- 11. Find an approximate value of a real root of the equation $x^3 x 1 = 0$ by the bisection method.
- 12. Find a cubic polynomial which takes the following values: y(1) = 24, y(3) = 120, y(5) = 336, y(7) = 720.
- 13. Given $\frac{dy}{dx} = x^2 + y$; y(0) = 1, compute y(0.02) using Euler's modified method. (7×2=14)

SECTION - College and the second residence of the seco

Answer any 4 questions from among the questions 14 to 19. These questions carry 3 marks each.

- 14. Find the length of the circular helix $r(t) = [2 \cos t, 2 \sin t, 6t]$ from (2, 0, 0) to $(2, 0, 24\pi)$.
- 15. Evaluate $\iint_S F \cdot n \, dA$ by the divergence theorem where F = [4x, 3z, 5y], S the surface of the cone $x^2 + y^2 \le z^2$, $0 \le z \le 2$.



16. Using Lagrange's interpolation formula, find the form of the function y(x) from the following table :

X	0	1	3	4	
у	-12	0	12	24	

- 17. Explain Simpson's 1/3-rule for numerical integration.
- 18. Use Newton-Raphson method to find a root of the equation $x^3 2x 5 = 0$.
- 19. Given y'' xy' y = 0; y(0) = 1, y'(0) = 0, use Taylor's series method to determine y(0.1), correct to four decimal places. (4x3=12)

SECTION - D

Answer any 2 questions from among the questions 20 to 23. These questions carry 5 marks each.

- 20. Show that the helix [a cos t, a sin t, ct] can be represented by [a cos(s / K), a sin(s / K), cs/K] where $K = \sqrt{a^2 + c^2}$ and s is the arc length. Show that it has constant curvature $K = a / K^2$ and torsion $T = c / K^2$.
- 21. Verify Stokes's theorem for $F = \left[z^2, \frac{3}{2}x, 0\right]$, S the square $0 \le x \le a, 0 \le y \le a, z = 1$.
- 22. From the following table of values of x and y, obtain $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ for x = 1.2.

x	1.0	1.2	1.4	1.6	1.8	2.0	2.2
y	2.7183	3.3201	4.0552	4.9530	6.0496	7.3891	9.0250

23. Given, $\frac{dy}{dx} = 1 + y^2$; y(0) = 0, use Runge-Kutta method with h = 0.2, to find y(0.2), y(0.4) and y(0.6). (2x5=10)